

Code No: 52120/MT

**M.Tech. – I Semester Supplementary Examinations,
September, 2008**

MODERN CONTROL THEORY
(Common to Power Electronics/ Electrical Power Engineering/
Power Engineering & Energy Systems)

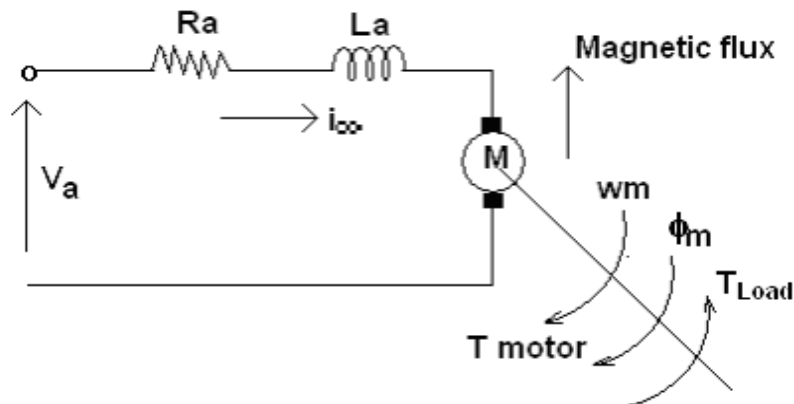
Time: 3 hours

Max. Marks:60

Answer any FIVE questions
All questions carry equal marks

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- 1.a) Define the following
 i) Eigen values ii) Eigen vectors ii) State of a system
 b) Consider the system shown for the d.c. motor



Obtain the state space model. Obtain its state diagram and also the block diagram.

- 2.a) Explain the properties of state transition matrix.
 b) Find $x_1(t)$ and $x_2(t)$ of the system described by

$$\begin{bmatrix} \dot{x}_1(t) \\ \dot{x}_2(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -3 & -2 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

Where the initial condition are

$$\begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

Contd...2

- 3.a) Explain with an example the concept of controllability in continuous time invariant systems.
- b) Show that the dynamic system described by the following equation with usual notation is completely output controllable if and only if the composite $[m \times nr]$ matrix P_1 where
- $$[P] = [CB : CAB : CA^2B : \dots : CA^{n-1}B]$$
- is of rank m .
- $$\dot{\underline{x}} = [A]\underline{x} + [B]\underline{u}$$
- $$\underline{y} = [C]\underline{x}$$
- 4.a) What are the various types of non-linearities that occur in control systems. What are their characteristics and effects on the operations of a control system.
- b) What is a describing function? Explain how an element with dead-zone can be analysed using describing function method.
- 5.a) What are singular points and how are they classified. Sketch them and explain
- b) Explain how phase plane trajectory using method of isoclines can be constructed for the system described by $\frac{d^2x}{dt^2} + \frac{dx}{dt} + x(t) = 0$
- 6.a) Explain the terms-stability in the sense of Liapunov, asymptotic stability and instability with graphic representation.
- b) State and prove the Liapunov's stability theorem for linear time invariant systems.
- 7.a) Explain the method of control system design by pole placement.
- b) What are state observers? Explain. Sketch the block diagram of full order state observer.
- 8.a) Explain the fixed end point problem and derive the euler-Lagrange equation.
- b) Explain the term-Linear quadratic regulator.